

KVL Procedure

Consider the circuit shown at right.

1. Count the number of branches. You could think of this as counting the number of *unique* pipes for water to flow in the circuit.
 - a. Junctions with three or more pipes indicate the beginning or end of a branch.
 - b. A branch (or pipe) that turns 90° is still the same branch.
 - c. Generally one must include branches with no circuit elements (resistors, batteries, capacitors, switches, etc). In the example at right, the diagonal branch is an example of a branch with no circuit elements.
 - d. The circuit at right has 7 branches.
2. Label currents in each branch (i_1, i_2, i_3, \dots etc).
 - a. I sometimes use i_0 for special branches. In the circuit at right I might use i_0 for the diagonal branch with no circuit elements.
 - b. Try to be consistent in the directions you choose.
 - i. I like to choose away from the plus terminal of a battery.
 - ii. Dom usually chooses to the right or down.
3. Count the number of *interior* loops.
 - a. I call a loop interior if the loop has no branches inside of it.
 - b. The circuit in our example has 4 loops.
 - c. Notice each loop is labeled with a direction.
 - i. I usually like my loop directions to be directed out of the plus terminal of a battery if possible.
 - ii. Dom usually tends to go clockwise.
4. Determine the number of linearly independent junction equations.
 - a. (# of Branches) – (# of Loops) = (# of Junction Equations)
 - b. The circuit at right requires $7 - 4 = 3$ junction equations.
 - c. For each junction the sum of input currents should equal the sum of the output currents.
 - d. The junctions chosen are arbitrary.
5. Determine the loop equations.
 - a. The sum of *voltage gains* around a loop should equal zero (consequence of energy conservation).
 - b. Pick a spot to start on each loop and follow the chosen loop direction.
 - c. *Add* voltage gained across a battery if exiting on the *plus* terminal (subtract if exiting on the *minus* terminal).
 - d. *Subtract* iR when passing by a resistor *if loop direction matches current direction drawn*. Add iR if loop direction is opposite current direction drawn.
 - e. These rules reflect that (1) batteries are used to *add* voltage to a circuit while (2) resistors tend to *decrease* the voltage available to other circuit elements. It is for these reasons we often call the potential difference across a resistor a voltage *drop*.
6. Do algebra to determine unknowns.
 - a. A problem typically involves the same number of unknowns as the number of branches.
 - b. Usually the currents are the unknowns.
 - c. On occasion, one of the currents is known while a resistance or battery voltage is unknown.
7. Interpret the results.
 - a. It is common to inaccurately predict the direction of a current...this is NOT a problem!
 - b. If you get a negative value for a current, the direction current flows in real life is opposite the direction you chose to draw it!

